

Trasformate di Laplace.

$f(t)$	<i>causale</i>	$F(s) = \mathcal{L}(f)(s) = \int_0^{+\infty} f(t)e^{-st} dt$	
	$H(t)$	$\frac{1}{s}$	
	$H(t)t^n$	$\frac{n!}{s^{n+1}}$	$n \in \mathbb{N}$
	$H(t)e^{\lambda t} \frac{t^{\alpha-1}}{\Gamma(\alpha)}$	$\frac{1}{(s-\lambda)^\alpha}$	$\operatorname{Re} \alpha > 0, \lambda \in \mathbb{C}$
	$H(t) \frac{e^{\alpha t} - e^{\beta t}}{\alpha - \beta}$	$\frac{1}{(s-\alpha)(s-\beta)}$	$\alpha, \beta \in \mathbb{C}, \alpha \neq \beta$
	$H(t) \sin \omega t$	$\frac{\omega}{s^2 + \omega^2}$	$\omega \neq 0$
	$H(t) \cos \omega t$	$\frac{s}{s^2 + \omega^2}$	$\omega \neq 0$
	$H(t) \sinh \omega t$	$\frac{\omega}{s^2 - \omega^2}$	$\omega \neq 0$
	$H(t) \cosh \omega t$	$\frac{s}{s^2 - \omega^2}$	$\omega \neq 0$
	$H(t) \log t$	$\frac{\Gamma'(1) - \log s}{s}$	
	$H(t)e^{-t^2}$	$\frac{\sqrt{\pi}}{2} e^{s^2/4} \operatorname{erfc}(s/2)$	
	$H(t) \operatorname{erf}(t)$	$\frac{1}{s} e^{s^2/4} \operatorname{erfc}(s/2)$	
	$H(t) \operatorname{erf}(\sqrt{t})$	$\frac{1}{s\sqrt{s+1}}$	
	$H(t)J_0(at)$	$\frac{1}{\sqrt{s^2 + a^2}}$	$a > 0$
	$H(t)J_0(2\sqrt{at})$	$\frac{e^{-s/a}}{s}$	$a > 0$

La funzione Γ di Eulero.

$$\begin{aligned}\Gamma(\lambda) &:= \int_0^{+\infty} t^{\lambda-1} e^{-t} dt, \quad \operatorname{Re} \lambda > 0; \\ \Gamma(\lambda + 1) &= \lambda \Gamma(\lambda), \quad \lambda \in \mathbb{C} \setminus \{0, -1, -2, \dots, -n, \dots\} \\ \Gamma(n) &= (n-1)! \quad n = 1, 2, \dots \\ \Gamma(\tfrac{1}{2}) &= \sqrt{\pi}, \quad \Gamma(n + 1/2) = \frac{1 \cdot 3 \cdot 5 \dots (2n-1)}{2^n} \sqrt{\pi} = \frac{(2n)!}{2^{2n} n!} \sqrt{\pi} \\ \Gamma(\lambda) \Gamma(1-\lambda) &= \frac{\pi}{\sin \pi \lambda} \\ \Gamma'(1) &= -\gamma = \lim_{n \uparrow +\infty} \left(\log n - \sum_{k=1}^n \frac{1}{k} \right)\end{aligned}$$

Error functions

$$\operatorname{erf} t = \frac{2}{\sqrt{\pi}} \int_0^t e^{-s^2} ds, \quad \operatorname{erfc} t = 1 - \operatorname{erf} t = \frac{2}{\sqrt{\pi}} \int_t^{+\infty} e^{-s^2} ds$$

Funzioni di Bessel.

$$\begin{aligned}J_\nu(t) &:= \sum_{n=0}^{+\infty} (x/2)^\nu \frac{(-1)^n (x/2)^{2n}}{n! \Gamma(n + \nu + 1)} \\ J_\nu'' + \frac{1}{t} J_\nu' + \left(1 - \frac{\nu^2}{t^2}\right) J_\nu &= 0\end{aligned}$$